ELECTRONIC CALCULATORS MUST NOT BE USED IN THIS PAPER

1 **(a)** The temperature was $-2\,°C$.
The temperature decreases by $8\,°C$.

Find the temperature after this change.

.... °C [1]

(b) On another day, the temperature increases from $-5\,°C$ to $3\,°C$.

Work out the increase in temperature.

.... °C [1]

2 Find 45% of $1.20 .

$ .... [2]

3 Write these fractions in order of size, starting with the smallest.

$$\frac{11}{12} \qquad\qquad \frac{4}{5} \qquad\qquad \frac{27}{30} \qquad\qquad \frac{13}{15}$$

.... , ... , ... , ... [2]
smallest

4

North

A

North

B
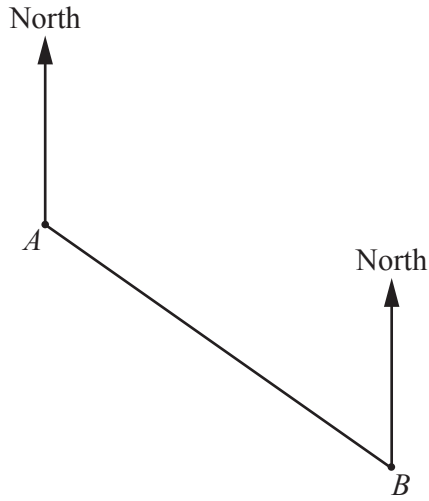
Scale: 1 cm to 30 m

The diagram shows the position of two ships, *A* and *B*.
On the diagram 1 cm represents 30 m.

(a) Find, by measurement, the actual distance of *B* from *A*.

.... m [2]

(b) Measure the bearing of *B* from *A*.

.... [1]

(c) A third ship is positioned at *C*.
C is on a bearing of 164° from *A* and on a bearing of 252° from *B*.

Find and label the position of *C* on the diagram. [2]

5 **(a)** Write 306.248

    (i) correct to 2 decimal places,

.... [1]

    (ii) correct to 2 significant figures.

.... [1]

(b) By writing each number correct to 1 significant figure, estimate the value of

$$9.37^2 - \sqrt[3]{1046} \ .$$

.... [2]

6 **(a)** Write $4 \times 4 \times 4 \times 4 \times 4$ as a power of 4.

.... [1]

(b) Simplify $\left(\sqrt{5}\right)^2$.

.... [1]

(c) Simplify $\left(2x^3\right)^4$.

.... [1]

7 **(a)** Work out $\dfrac{7}{8} - \dfrac{3}{4}$.

.... [1]

(b) Work out $1\dfrac{3}{5} \div \dfrac{4}{7}$.

Give your answer as a mixed number in its lowest terms.

.... [2]

8 Factorise $3a^2 + 12a$.

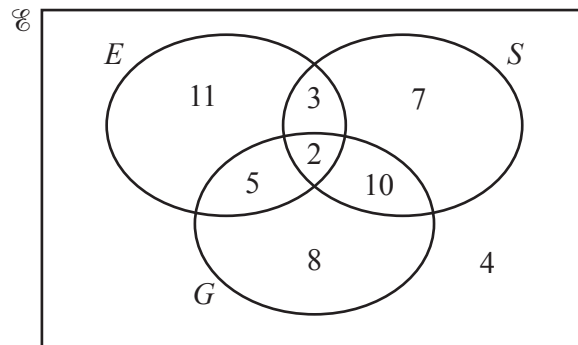.. [2]

9 **(a)** In the Venn diagram, shade the region represented by $A \cap B$.
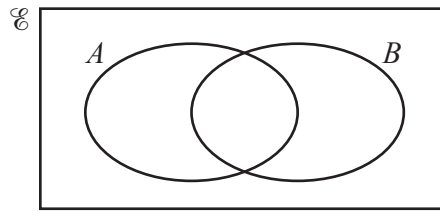
[1]

(b) This Venn diagram shows information about the number of students who study English (E), Spanish (S) and German (G).

(i) Find the number of students who study English and German but not Spanish.

.... [1]

(ii) Find $n(G \cup S)'$.

.... [1]

10 (a) Write the number 320 000 000 in standard form.

.... [1]

(b) Evaluate $\dfrac{2 \times 10^{-3}}{4 \times 10^9}$.

Give your answer in standard form.

.... [2]

11 (a) Write 120 as a product of its prime factors.

.... [2]

(b) $$315 = 3^2 \times 5 \times 7$$

Use this information to find the smallest integer value of *n*, such that 315*n* is a square number.

.... [1]

12 Expand and simplify.

(a) $3(2x+1)-2(4x+3)$

.... [2]

(b) $(x+5)(x-3)$

.... [2]

13 (a) The nth term of a sequence is $3n^2-1$.

Find the first three terms of the sequence.

.... , ... , ... [2]

(b) These are the first five terms of a different sequence.

$$1 \quad 3 \quad 9 \quad 27 \quad 81$$

Find an expression, in terms of n, for the nth term of this sequence.

.... [2]

14
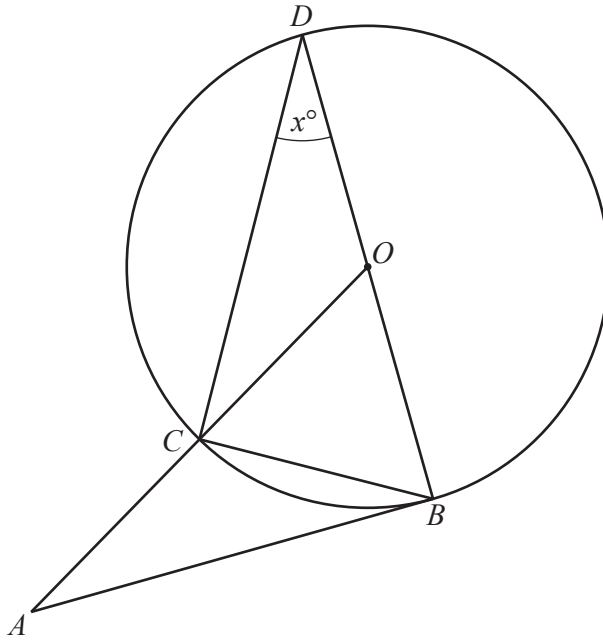
NOT TO
SCALE

B, C and D are points on the circumference of a circle, centre O.
AB is a tangent to the circle at B.
BD is a diameter and OCA is a straight line.
$C\hat{D}B = x°$.

Find an expression, in terms of x, for each of the following.
Write each expression in its simplest form.

(a) $C\hat{O}B$

$C\hat{O}B = $ .... [1]

(b) $O\hat{A}B$

$O\hat{A}B = $ .... [2]

(c) $C\hat{B}O$

$C\hat{B}O = $ .... [2]

     [Turn over

15
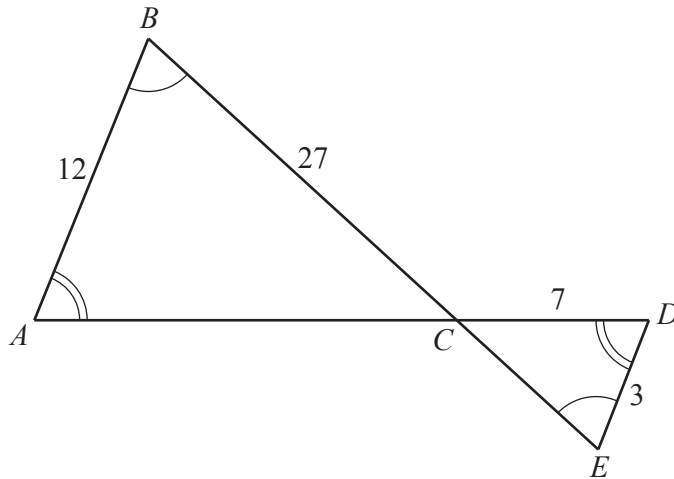
NOT TO
SCALE

Triangle *ABC* is mathematically similar to triangle *DEC*.
AB = 12 cm, *BC* = 27 cm, *CD* = 7 cm and *DE* = 3 cm.

(a) Calculate *AC*.

.... cm [2]

(b) Given that the area of triangle *ABC* is 160 cm^2, calculate the area of triangle *DEC*.

.... cm^2 [2]

16
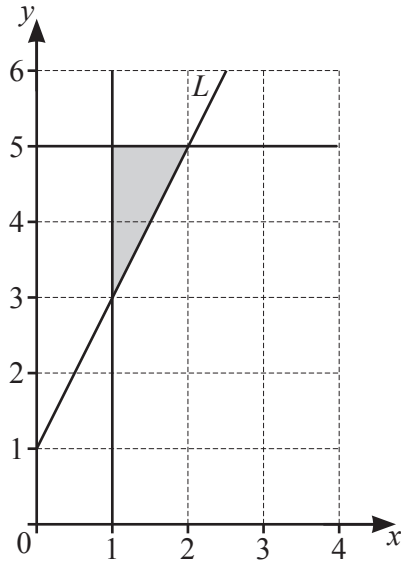
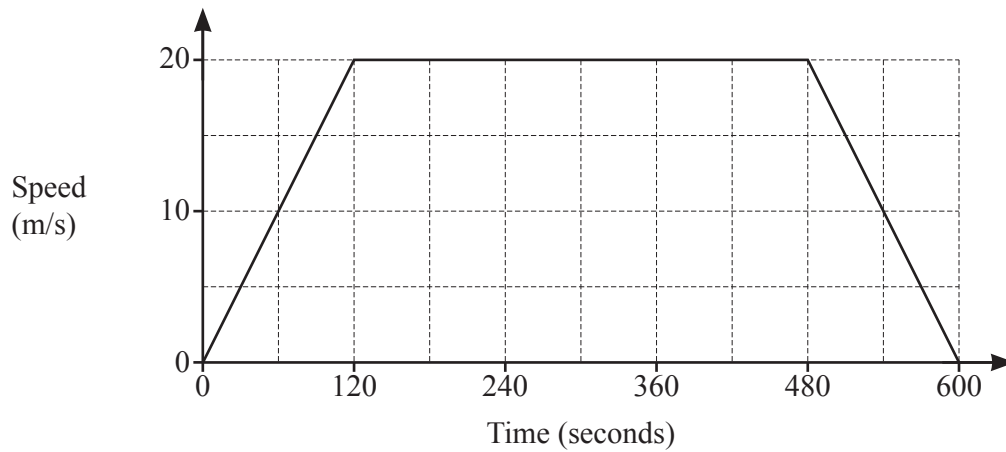**(a)** Find the gradient of the line L.

.... [1]

(b) The shaded region on the diagram is defined by three inequalities.

Write down these three inequalities.

....

....

.... [3]

17 The diagram shows the speed–time graph of Sam's journey from home to work.

(a) Calculate the acceleration, in m/s^2, for the first 2 minutes of Sam's journey.

.... m/s^2 [1]

(b) Calculate Sam's average speed, in m/s, for the whole journey.

.... m/s [3]

18 *b* is directly proportional to the square of *a*.
When $a = 3$, $b = 18$.

Find *b* when $a = 5$.

$b = $ .... [2]

19
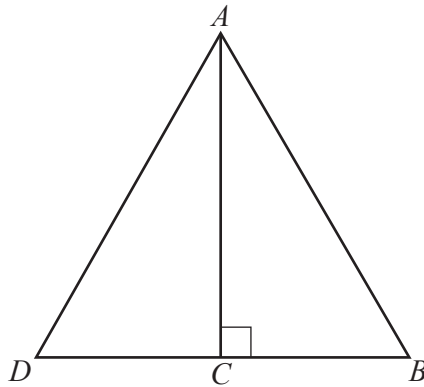
ABD is an equilateral triangle.
C lies on *DB* and *AC* is perpendicular to *DB*.

Show that triangle *ADC* is congruent to triangle *ABC*.
Give a reason for each statement you make.

....

....

....

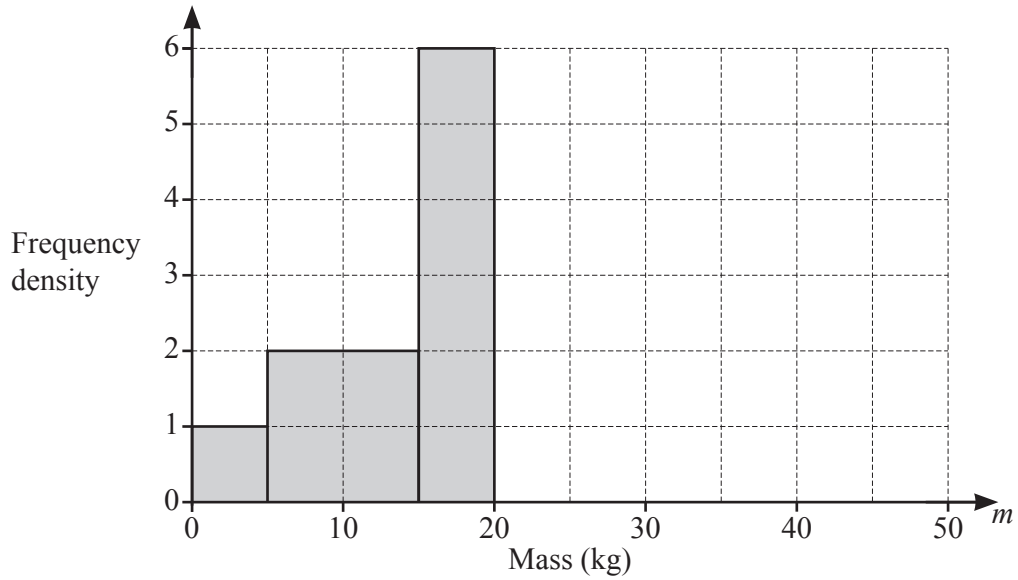... [3]

20 A farmer records the mass of each of his sheep.
Some of the results are summarised in the table and illustrated in the histogram.

Mass (m kg)	$0 < m \leqslant 5$	$5 < m \leqslant 15$	$15 < m \leqslant 20$	$20 < m \leqslant 30$	$30 < m \leqslant 50$
Frequency	5	20	a	40	20

(a) Use the histogram to find the value of a.

$a =$ .... [1]

(b) Complete the histogram. [2]

21 $\mathbf{A} = \begin{pmatrix} 3 & 1 \\ -4 & 2 \end{pmatrix}$ $\mathbf{A} + 2\mathbf{B} = \begin{pmatrix} 1 & 5 \\ 10 & 12 \end{pmatrix}$

   (a) Find **B**.

$\left(\quad\quad \right)$ [2]

   (b) Find $\mathbf{A}^{-1}$.

$\left(\quad\quad \right)$ [2]

$\mathbf{A} = \begin{pmatrix} 3 & 1 \\ -4 & 2 \end{pmatrix}$ $\mathbf{A} + 2\mathbf{B} = \begin{pmatrix} 1 & 5 \\ 10 & 12 \end{pmatrix}$

22 (a) $x^2 - 6x - 7 = (x + a)^2 + b$

Find the value of a and the value of b.

$a =$ ....

$b =$ .... [2]

(b) Hence solve the equation $x^2 - 6x - 7 = 0$.
Show your working.

$x =$ .... or $x =$ .... [2]

23 [Volume of a cone $= \frac{1}{3}\pi r^2 h$, curved surface area of a cone $= \pi r l$]

[Surface area of a sphere $= 4\pi r^2$]

A solid cone has radius y cm.
The slant height of the cone is 25% larger than the radius of the cone.

A solid sphere has radius R cm.
The surface area of the sphere is equal to the **total** surface area of the cone.

(a) Show that $y = \dfrac{4R}{3}$.

[3]

(b) Find the volume of the cone in terms of R.
Give your answer as simply as possible.

.... cm^3 [4]

4024/11/O/N/22